

Mark Scheme (Results)

January 2022

Pearson Edexcel International Advanced Level In Mechanics M3 (WME03) Paper 01

Edexcel and BTEC Qualifications

Edexcel and BTEC qualifications are awarded by Pearson, the UK's largest awarding body. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information visit our qualifications websites at www.edexcel.com or www.edexcel.com, you can get in touch with us using the details on our contact us page at www.edexcel.com/contactus.

Pearson: helping people progress, everywhere

Pearson aspires to be the world's leading learning company. Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for our commitment to high standards and raising achievement through innovation in education. Find out more about how we can help you and your students at: www.pearson.com/uk

January 2022

Question Paper Log Number P72404A

Publications Code WME03_01_2201_MS

All the material in this publication is copyright

© Pearson Education Ltd 2022

General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
 - M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise
 indicated.
 - Amarks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - **B** marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{\text{will}}$ be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.

- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

General Principles for Mechanics Marking

(But note that specific mark schemes may sometimes override these general principles)

- Rules for M marks: correct no. of terms; dimensionally correct; all terms that need resolving (i.e. multiplied by cos or sin) are resolved.
- Omission or extra g in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- DM indicates a dependent method mark i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of g = 9.8 should be given to 2 or 3 SF.
- Use of g = 9.81 should be penalised once per (complete) question.
 - N.B. Over-accuracy or under-accuracy of correct answers should only be penalised *once* per complete question. However, premature approximation should be penalised every time it occurs.
- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c),.....then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft
- Mechanics Abbreviations

M(A) Taking moments about A.

N2L Newton's Second Law (Equation of Motion)

NEL Newton's Experimental Law (Newton's Law of Impact)

HL Hooke's Law

SHM Simple harmonic motion

PCLM Principle of conservation of linear momentum

RHS, LHS Right hand side, left hand side.

Question Number	Scheme	Marks
1.	Area = $\int_0^a (x^2 + ax) dx = \left[\frac{1}{3} x^3 + \frac{1}{2} ax^2 \right]_0^a = \frac{5a^3}{6}$	M1A1
	$\int \frac{1}{2} y^2 dx = \int_0^a \frac{1}{2} (x^4 + 2ax^3 + a^2x^2) dx$	M1
	$= \frac{1}{2} \left[\frac{1}{5} x^5 + \frac{a}{2} x^4 + \frac{a^2}{3} x^3 \right]_0^a \left(= \frac{31a^5}{60} \right)$	DM1A1
	$\overline{y} = \frac{\int \frac{1}{2} y^2 dx}{\int y dx} = \frac{31a^5}{60} \div \frac{5a^3}{6} = \frac{31a^2}{50}$	M1A1 (7)
		[7]
M1 A1	Attempt the area by integration. Powers of both terms to increase by 1. Correct area.	
M1	Use $\int \frac{1}{2} y^2 dx$ to give $\int_0^2 \frac{1}{2} (x^4 + 2ax^3 + a^2x^2) dx$. Limits not needed. Squaring to	be correct. For
DM1 A1	method mark, condone missing $\frac{1}{2}$ or any multiple. Attempt the integration (powers of at least 2 terms to increase by 1). Depends on second M mark. Correct integration and correct limits shown. Limits needed but substitution does not need to be seen.	
M1	Use $\overline{y} = \frac{\int \frac{1}{2} y^2 dx}{\int y dx}$	
A1	Note: This independent method mark is for use of the correct formula. Correct answer.	

Question Number	Scheme	Marks	
2	Any correct sin or cos ratio.	B1	
	$T\cos 60^{\circ} + N = mg$	M1A1	
	$T\sin 60^\circ = mr\omega^2 = m\omega^2 \times 2l\sin 60^\circ$	M1A1	
	$\frac{1}{2}T + N = mg \qquad \frac{1}{2}T = ml\omega^2$		
	$\Rightarrow ml\omega^2 + N = mg$	DM1	
	$N \ge 0 \Rightarrow l\omega^2 \le g$	DM1	
	$\omega \leq \sqrt{\frac{g}{l}} *$	A1 * (8) [8]	
B1 M1 A1 M1 A1 DM1	May be seen explicitly or used in an equation. Attempt at vertical resolution, 3 terms needed. Correct equation. Attempt an equation for NL2 along the radius, acceleration in either form but not 'a'. May have r and v in the equation. Fully correct equation with the acceleration in $r\omega^2$ form and radius in terms of l . Eliminate T Depends on both M marks above. Must see an equation still involving N .		
DM1	Use $N \ge 0$ Depends on all 3 M marks above. Must see correct inequality stated, not $N = 0$ or $N > 0$.		
A1*	Reach the given result from fully correct working.		
ALT	For solutions that do not use vertical equilibrium but go straight to a vertical inequality.		
B1 M1 A1 DM1 M1 A1 DM1 A1*	As above. Forming a correct inequality $T\cos 60 \le mg$ Attempt NL2 as the main mark scheme. Eliminate T Depends on M marks above. Reach the given result from fully correct working.		

Question Number	Scheme	Marks
3		
(a)	$mv\frac{\mathrm{d}v}{\mathrm{d}x} = mg\sin\alpha - \frac{1}{3}mx^2$	M1A1
	$\frac{1}{2}v^2 = xg\sin\alpha - \frac{1}{9}x^3 \ (+c)$	DM1A1
	$x = 2 \frac{1}{2}v^2 = 2g\sin\alpha - \frac{8}{9}$	DM1
	(v = 3.728) v = 3.7 or 3.73 (m s ⁻¹)	Alcso (6)
ALT	By energy:	
	$mg\sin\alpha x = \int \frac{1}{3}mx^2 dx + \frac{1}{2}mv^2$	M1A1
	$xg\sin\alpha = \frac{1}{9}x^3 + \frac{1}{2}v^2(+c)$	DM1A1
	$x = 2$ $\frac{1}{2}v^2 = 2g \sin \alpha - \frac{8}{9}$	DM1
	$v = 3.7 \text{ or } 3.73 \text{ (m s}^{-1})$	A1
(b)	$v = 0 \Rightarrow x^2 = 9g \sin \alpha = 9g \times \frac{2}{5} (x \neq 0)$	
	$x = 5.939 \Rightarrow OA = 5.9 \text{ or } 5.94 \text{ (m)}$	M1A1 (2) [8]

Question Number	Scheme	Marks
(a) M1	Attempt an equation of motion parallel to the plane with acceleration in any for	rm (including a)
A1	Correct equation with the acceleration in $v \frac{dv}{dx}$ form	
DM1	Attempt the integration, powers increase by 1 in 2 terms – the constant may be missing. Acceleration must be in $v \frac{dv}{dx}$ form.	
A1	Correct integration.	
DM1 A1	Sub $x = 2$ in their expression for v^2 Depends on all previous M marks. Correct value for v and $+c$ should be dealt with. Must be 2 or 3 sf	
ALT M1 A1	Attempt a 3 term energy equation – KE, GPE, work done. Integral form is not required here. Fully correct equation with integral form for work done. Rest as main scheme.	
(b) M1 A1	Use $v = 0$ in their expression for v and obtain a value of x Correct value of length OA . (Allow if x instead of OA) Must be 2 or 3 sf (unless already penalised in (a)	
ALT (b) M1 A1	Start again with energy and integrate to obtain a value of <i>x</i> See mark scheme.	

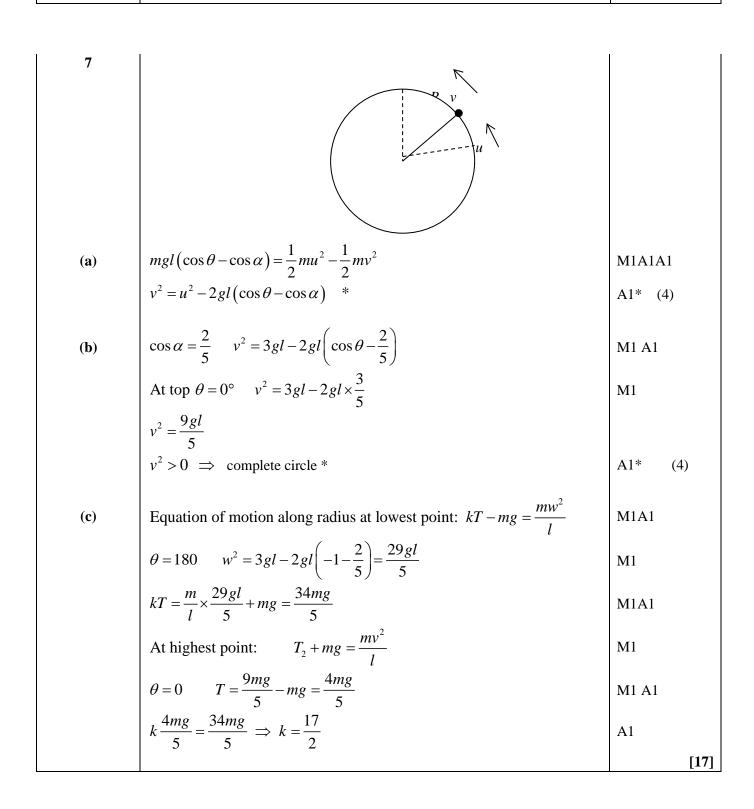
Question Number	Scheme	Marks	
4(a)	Ratio of masses: $4\pi a^2$ $4\pi a \times ka$ $8\pi a^2$ $12\pi a^2 + 4k\pi a^2$	B1	
	Distances: $(0) \frac{k}{2}a (1+k)a \overline{y}$	B1	
	$(0+)k \times \frac{k}{2}a + 2(1+k)a = (k+3)\overline{y}$	M1A1ft	
	$\left(\frac{k^2}{2} + 2 + 2k\right)a = (k+3)\overline{y}$		
	$\overline{y} = \frac{\left(k^2 + 4k + 4\right)}{2\left(k + 3\right)}a *$	A1 * (5)	
(b)	$\tan 60^{\circ} = \frac{\left(k^2 + 4k + 4\right)}{2\left(k + 3\right)}a \div 2a$	M1	
	$k^{2} + 4k\left(1 - \sqrt{3}\right) + \left(4 - 12\sqrt{3}\right) = 0$	A1	
	$k > 0 \implies k = 5.8147 = 5.8$ or 5.81 or better	A1 (3) [8]	
(a) B1 B1	Correct ratio of masses – any equivalent to that shown Correct distances from <i>O</i> or a parallel axis.		
M1	Attempt a moments equation. Must be dimensionally correct (not using volumextra terms.	mes) and have no	
A1ft A1* (b)	Correct equation, follow through their ratio of masses and distances Correct given expression with sufficient working		
M1	Use $\tan 60 = \frac{\overline{y}}{2a}$ or $\frac{2a}{\overline{y}}$ May also use $\tan 30$		
A1 A1	Obtain the correct 3TQ Correct value for k .		
	Note for (a):		
	The distance from O for the combined cylinder and base is $\frac{ak^2}{2(1+k)}$.		

Question Number	Scheme	Mar	ks
5(a)	$x = 4\cos\left(\frac{1}{5}\pi t\right) \dot{x} = -4 \times \frac{\pi}{5}\sin\left(\frac{1}{5}\pi t\right)$		
	$\ddot{x} = -4 \times \left(\frac{\pi}{5}\right)^2 \cos\left(\frac{1}{5}\pi t\right)$	M1A1	
	$\ddot{x} = -\left(\frac{\pi}{5}\right)^2 x :: SHM$	A1	(3)
(b)	period = $\frac{2\pi}{\frac{\pi}{5}}$ = 10 (s)	M1A1	(2)
(c)	amplitude = 4 (m)	B1	(1)
(d)	$\dot{x} = -4 \times \frac{\pi}{5} \sin\left(\frac{1}{5}\pi t\right) \text{or} \dot{x}_{\text{max}} = a\omega$	M1	
	Max speed = $4 \times \frac{\pi}{5} = \frac{4\pi}{5}$ or 0.8π (ms ⁻¹)	A1	(2)
(e)	At $A x = 1.5$ $1.5 = 4\cos\left(\frac{1}{5}\pi t\right)$ $\Rightarrow t_A = \frac{5}{\pi}\cos^{-1}\left(\frac{1.5}{4}\right)$	M1A1	
	At $B \ x = -2.5 \ -2.5 = 4\cos\left(\frac{1}{5}\pi t\right) \implies t_B = \frac{5}{\pi}\cos^{-1}\left(\frac{-2.5}{4}\right)$	A1	
	Time A to B = $t_B - t_A = \frac{5}{\pi} \cos^{-1} \left(\frac{-2.5}{4} \right) - \frac{5}{\pi} \cos^{-1} \left(\frac{1.5}{4} \right) = 1.6862 = 1.7 \text{ or better (s)}$	A1	(4)
(a)			[12
M1	Differentiate the given expression for x twice (Both derivatives must be show Need to see: cos to sin to cos (ignore signs)	vn)	
A1	Both derivatives correct		
A1	Rewrite in the standard form for SHM and give the conclusion.		
(b) M1	Correct method		
A1	Correct period		
(c)			
B1 (d)	Correct amplitude		
M1	Use either method to obtain the max speed		
A1	Correct max speed		
(e) M1	Find the time from the start to either <i>A</i> or <i>B</i>		
A1	One correct time		
	Second relevant time		
A1 A1	Correct time from A to B. 1.7 (s) or better		

Question Number	Scheme	Marks
ALT (e)	$1.5 = 4\sin\left(\frac{1}{5}\pi t\right) \implies t_A = \frac{5}{\pi}\sin^{-1}\left(\frac{1.5}{4}\right) $ M1A1	
	$2.5 = 4\sin\left(\frac{1}{5}\pi t\right) \implies t_B = \frac{5}{\pi}\sin^{-1}\left(\frac{2.5}{4}\right)$ A1	
	$_{A}t_{B} = t_{B} + t_{A} = \frac{5}{\pi}\sin^{-1}\left(\frac{2.5}{4}\right) + \frac{5}{\pi}\sin^{-1}\left(\frac{1.5}{4}\right) = 1.6862 \ 1.7 \text{ or better}$ A1	
6(a)	$T = \frac{\lambda x}{l} \Rightarrow 30 = \frac{\lambda \times 0.3}{0.5}$	M1A1
	$\lambda = 50 *$	A1* (3)
(b)	0.4 m <i>M</i>	
	0.3 m	
	Extension = 0.5 m (used in (b) or (c))	B1
	$T = \frac{50 \times 0.5}{0.5} = (50)$	M1A1ft
	$R(\uparrow) 2T\cos\theta - 1.2g = 1.2a$	M1
	$100 \times \frac{3}{5} - 1.2 \times 9.8 = 1.2a$	A1ft
	a = 40.2 $a = 40$ or 40.2 m s ⁻² (positive)	A1 (6)
(c)	E.P.E. = $\frac{1}{2} \times 50 \times \frac{0.5^2}{0.5}$	B1ft (any correct EPE)
	$1.2g \times 0.3 + \frac{1}{2} \times 1.2v^2 = \frac{1}{2} \times 50 \times \frac{0.5^2}{0.5} - \frac{1}{2} \times 50 \times \frac{0.3^2}{0.5}$	M1A1A1
	$v^{2} = \frac{1}{0.6} \left(25 \times \frac{0.5^{2}}{0.5} - 25 \times \frac{0.3^{2}}{0.5} - 1.2g \times 0.3 \right) (= 7.452)$	DM1
	$v = 2.730 = 2.7 \text{ or } 2.73 \mathrm{m s^{-1}}$	A1 (6)

Question Number	Scheme	Marks
		[15]
(a)		
M1	Use HL with $T = 30$	
A1	Correct equation	
A1*	Obtain given value for λ from fully correct working	
(b)		
B 1	Correct extension, seen explicitly or used in (b) or (c) Extension 0.25 if half st	ring used.
M1	Use HL to form an equation using $\lambda = 50$ and their extension.	-
A1ft	Correct equation, ft their extension	
M1	Attempt a vertical equation of motion. Must have 3 terms with T resolved a co	uld be negative.
A1ft	Correct equation with their value of T	
A1	Correct value of the acceleration (positive). Must be 2 or 3 sf.	
(c)		
B1ft	Either EPE correct, follow through their extension.	
M1	Energy equation, from C to the ceiling. PE, KE and 2 EPE terms required. EPE	E of the form $k \frac{x^2}{l}$
A1	Both EPE terms correct.	
A1 A1	Completely correct equation	
DM1	Solve for v^2 or v	
A1	Correct value for v. Must be 2 or 3 sf (unless penalised in (b)).	
	Control (1977)	

Question Number	Scheme	Marks
--------------------	--------	-------



Question Number	Scheme	Marks
--------------------	--------	-------

(a)	
M1	Attempt energy equation from A to general position. Must have a difference of 2 PE terms and a
	difference of 2 KE terms.
A1	Correct gain in PE or loss of KE
A1	Fully correct equation
A1*	Reach the given result from fully correct working
(b)	
M1	Sub $u = \sqrt{3gl}$ and $\cos \alpha = \frac{2}{5}$ in the result in (a)
A1	Correct equation
M1	Put $\theta = 0$ to find an expression for v^2 at the top (maybe finding KE)
A1*	Fully correct working and conclusion with reason eg reference to v^2 , v , KE
(c)	
M1	Form an equation of motion along the radius at the lowest point. Acceleration in either form.
A1	Correct equation with acceleration in v^2/r form
M1	Use $\theta = 180$ in result from (a) to obtain an expression for w^2
M1	Eliminate w^2 and obtain an expression for kT
A1	Correct expression for kT
M1	Form an equation of motion along the radius at the highest point. Acceleration in either form.
M1	Sub $\theta = 0$ and obtain an expression for T
A1	Correct expression for T
A1	Correct value of k. Must be exact.
NB	The equation of motion at the top may be seen first. Award M1A1 for either equation correct and M1 for the second.

Question Number	Scheme	Marks
ALT1 7(c)	Better equation of motion at top or bottom: $T - mg = \frac{mv^2}{l}$ $T + mg = \frac{mv^2}{l}$	M1 A1
	Other equation of motion – see above	M1
	Finding speed at the bottom: $\theta = 180 \qquad w^2 = 3gl - 2gl\left(-1 - \frac{2}{5}\right) = \frac{29gl}{5}$	M1
	Finding maximum Tension (lowest point) $\theta = 180, \ T = \frac{m}{l} \times \frac{29gl}{5} + mg = \frac{34mg}{5}$	M1 A1
	Finding minimum Tension (highest point) $\theta = 0 T = \frac{9mg}{5} - mg = \frac{4mg}{5}$	M1 A1
	Dividing Tensions to reach the correct answer $k \frac{4mg}{5} = \frac{34mg}{5} \implies k = \frac{17}{2}$	A1

Question Number	Scheme	Marks
ALT 2 7 (c)	General equation of motion: $T + mgcos\theta = \frac{mv^2}{l}$	M1 A1
	Use of $u = \sqrt{3gl}$ and $\cos \alpha = \frac{2}{5}$ to replace v^2 in their equation of motion	M1
	Finding speed at the lowest point: $\theta = 180 w^2 = 3gl - 2gl\left(-1 - \frac{2}{5}\right) = \frac{29gl}{5}$	M1
	Finding maximum Tension (lowest point) $\theta = 180, \ T = \frac{m}{l} \times \frac{29gl}{5} + mg = \frac{34mg}{5}$	M1 A1
	Finding minimum Tension (highest point) $\theta = 0, \ T = \frac{9mg}{5} - mg = \frac{4mg}{5}$	M1 A1
	Dividing Tensions to reach the correct answer $k \frac{4mg}{5} = \frac{34mg}{5} \implies k = \frac{17}{2}$	A1

Pearson Education Limited. Registered company number 872828 with its registered office at 80 Strand, London, WC2R 0RL, United Kingdom